

3
Exercise 2.2.12

a. Our definition of a convergent sequence that has a limit of zero requires, the sequence to have the following property:

$$(\forall \epsilon > 0)(\exists N)(\forall n \geq N)[|x_n - 0| < \epsilon]$$

The provided argument satisfies this requirement for only one ϵ , so we cannot call $x_n = (-1)^n$ a convergent sequence with a limit of zero.

b. The argument is valid, as it assumes $\langle x_n \rangle_n$ is eventually less than some epsilon, and a contradiction is found. The assumption being wrong precludes this sequence from being convergent with limit x by our definition.